

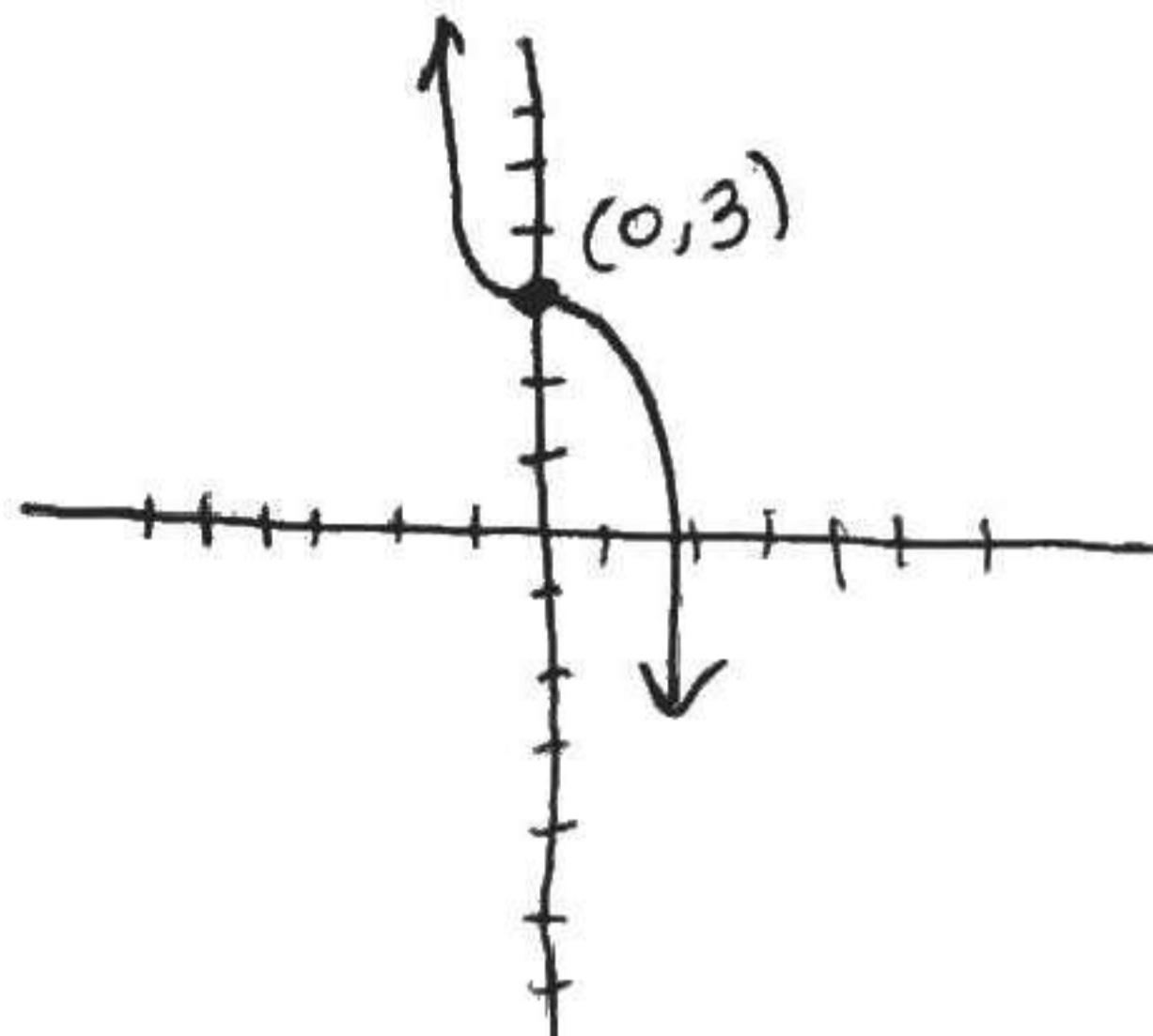
## Functional Analysis

### Chapter 4 Review (4.1-4.2)

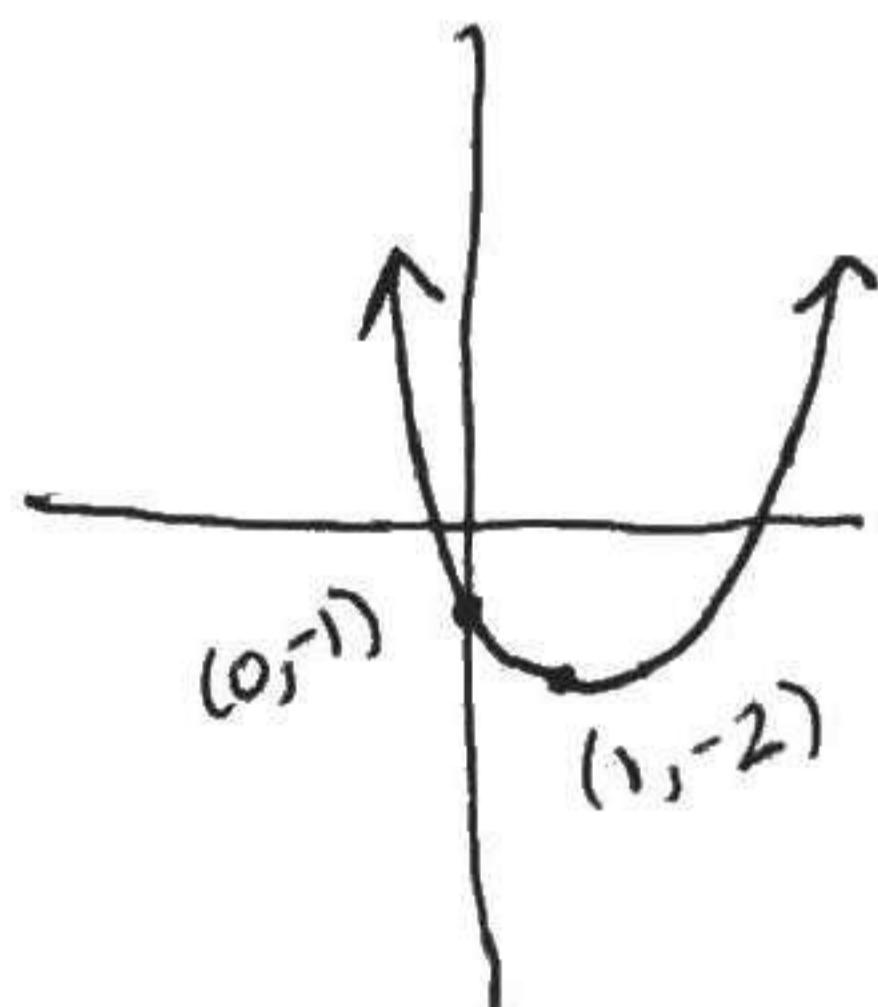
Name Key

In Problems 1 – 3, graph each function using transformations (shifting, compressing, stretching, and reflections). Show all the stages.

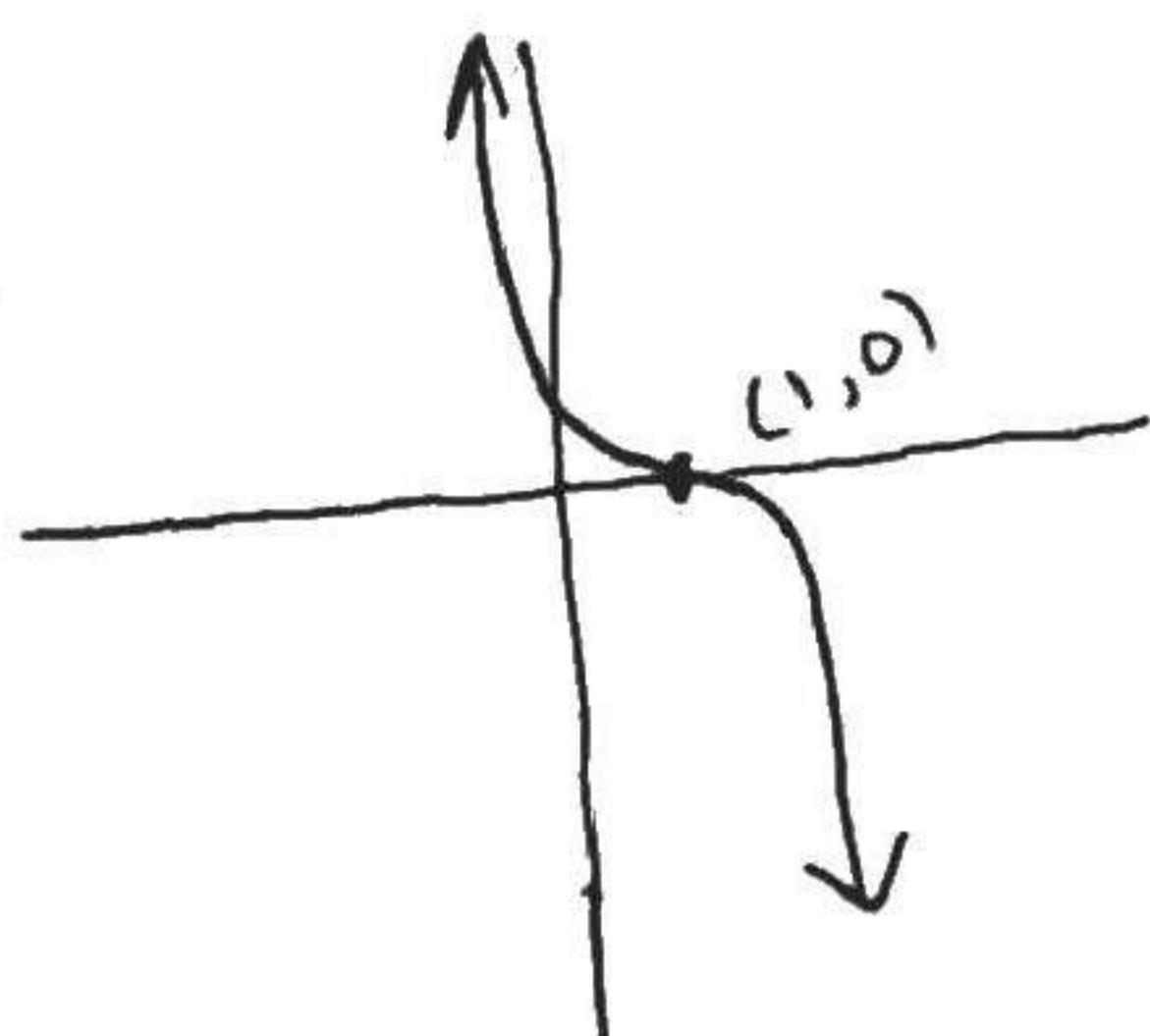
1.  $f(x) = -x^3 + 3$



2.  $f(x) = (x - 1)^4 - 2$

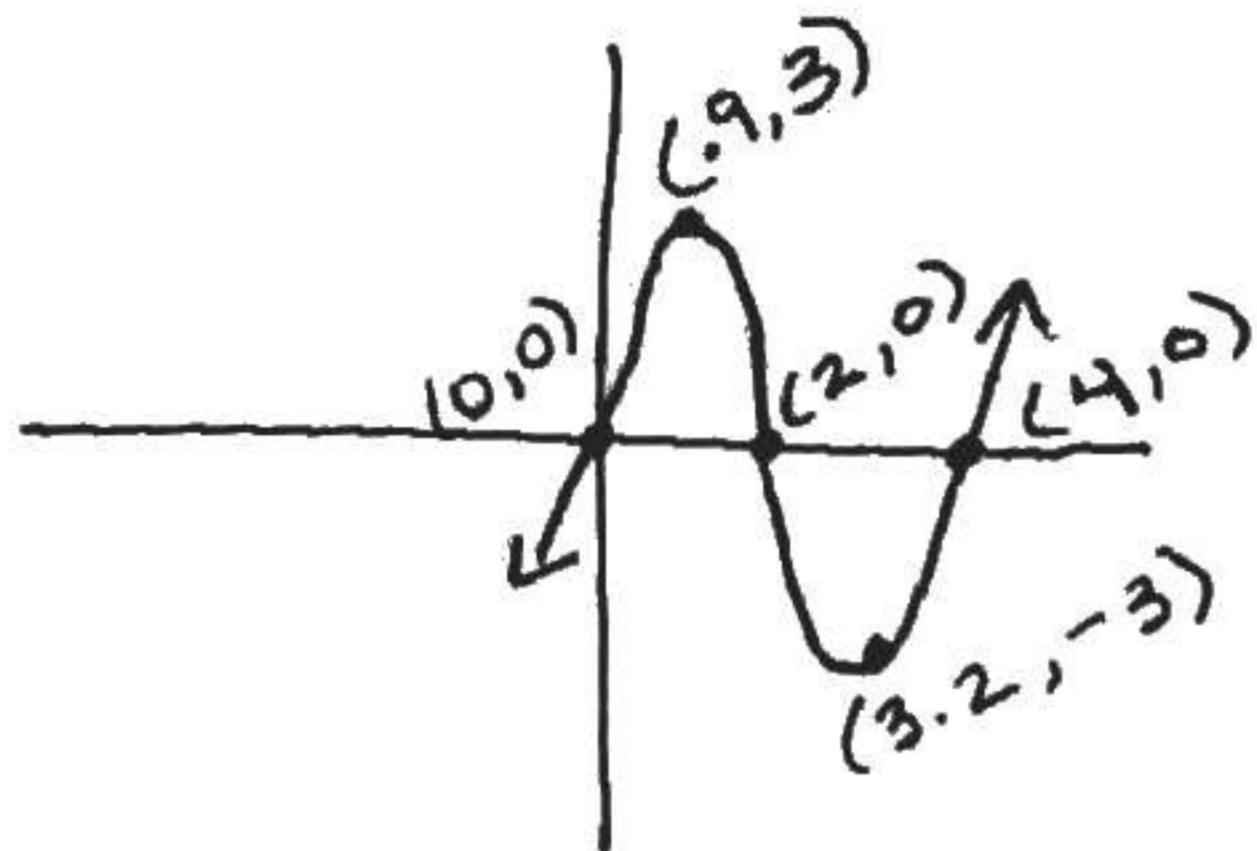


3.  $f(x) = (1 - x)^3$

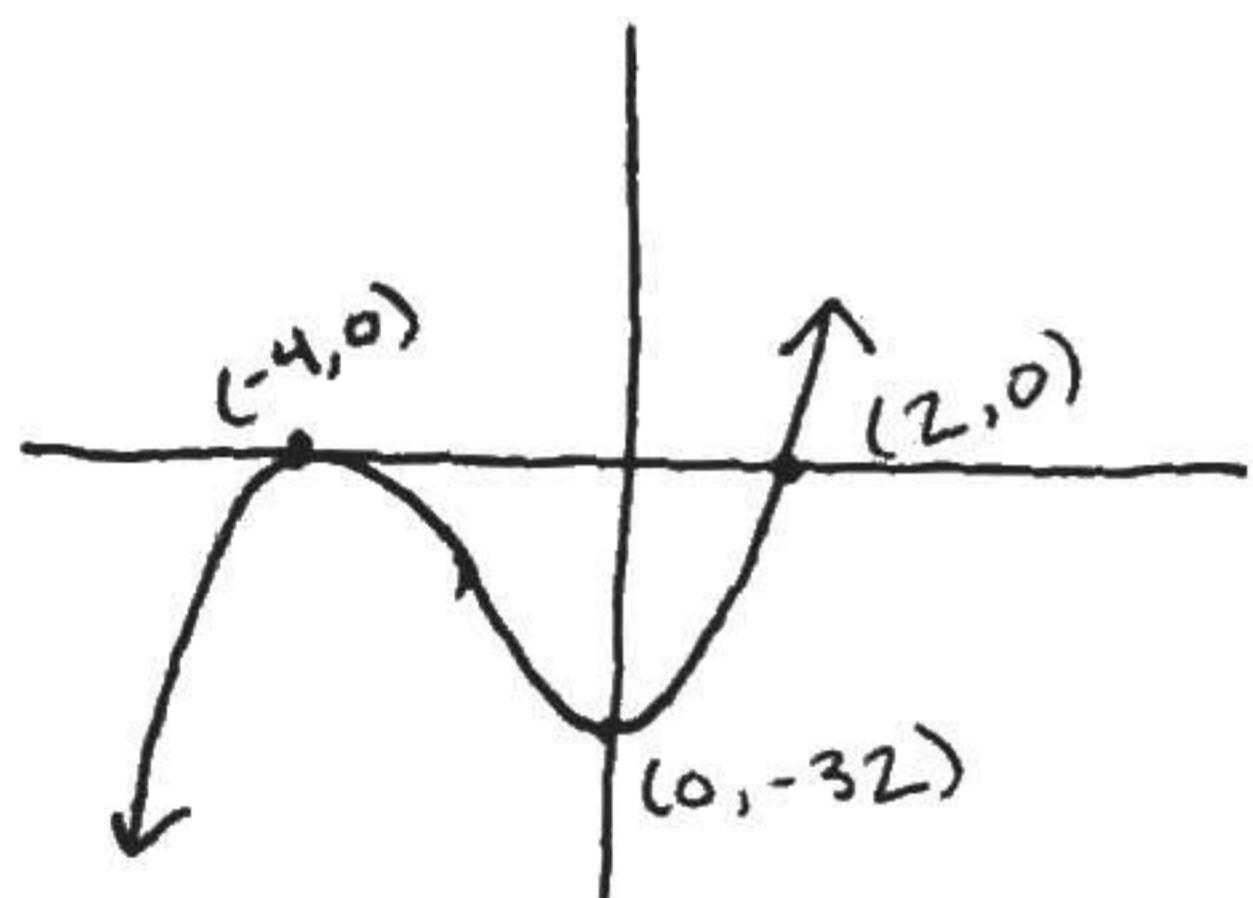


In Problems 4 – 7, analyze each polynomial by following Steps 1 through 8 on page 190.

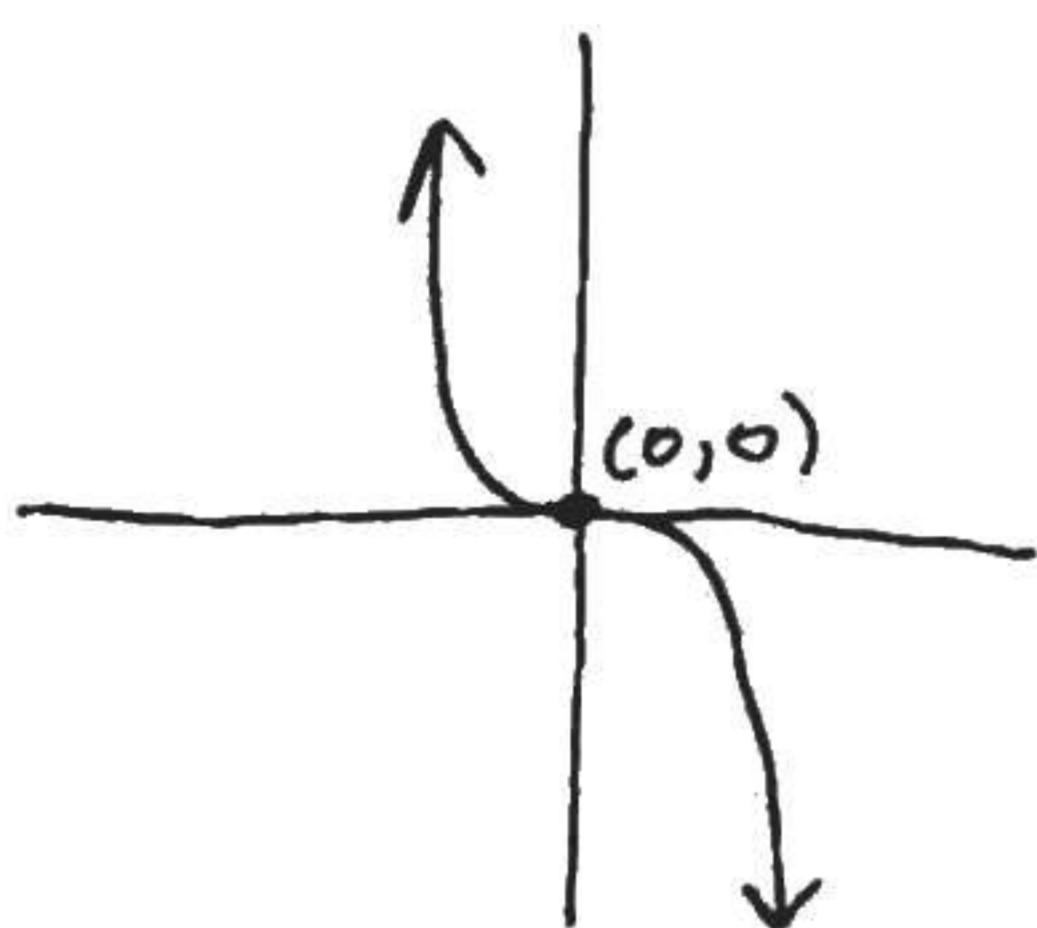
4.  $f(x) = x(x - 2)(x - 4)$



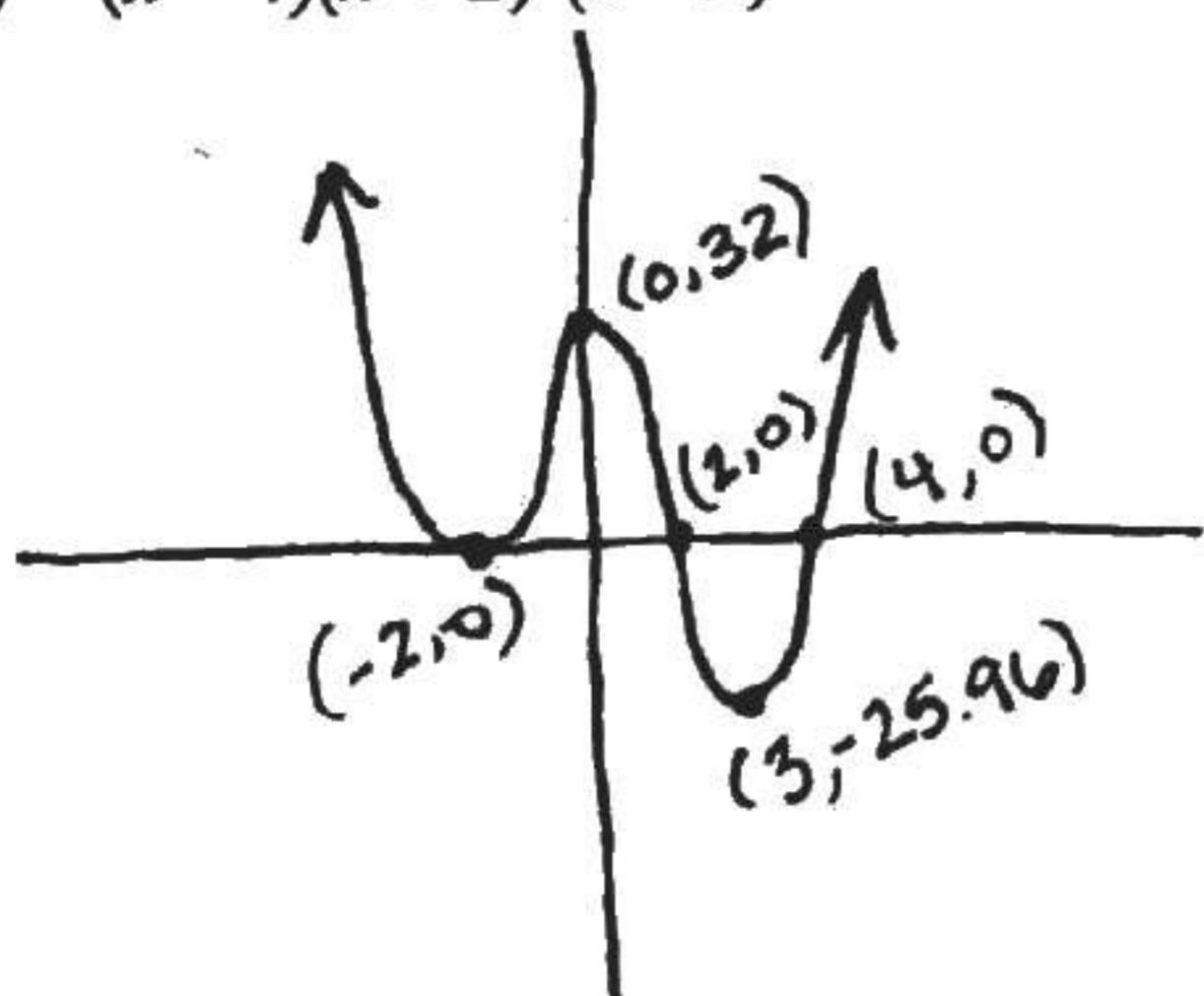
5.  $f(x) = (x - 2)(x + 4)^2$



6.  $f(x) = -4x^3 + 4x$



7.  $f(x) = (x - 4)(x + 2)^2(x - 2)$



In Problems 8 and 6, find the remainder  $R$  when  $f(x)$  is divided by  $g(x)$ . Is  $g$  a factor of  $f$ ?

8.  $f(x) = 2x^3 + 8x^2 - 5x + 5$ ;  $g(x) = x - 2$

$$\begin{array}{r} 2 \mid 2 \ 8 \ -5 \ 5 \\ \downarrow \quad 4 \ 24 \ 38 \\ \hline 2 \ 12 \ 19 \ 43 \end{array}$$

$$R = 43$$

9.  $f(x) = x^4 - x^2 + 2x + 2$ ;  $g(x) = x + 1$

$$\begin{array}{r} -1 \mid 1 \ 0 \ -1 \ 2 \ 2 \\ \quad \quad -1 \ 1 \ 0 \ -2 \\ \hline 1 \ -1 \ 0 \ 2 \ 0 \end{array}$$

$$R = 0$$

$(x+1)$  is a factor

10. Find the value of  $f(x) = -16x^3 + 18x^2 - x + 2$  at  $x = -2$ .

$$f(-2) = -16(-2)^3 + 18(-2)^2 - (-2) + 2 = 204$$

11. List all the potential rational zeros of  $f(x) = -6x^5 + x^4 + 2x^3 - x + 1$ .

$$Q = \pm 1, \pm 2, \pm 3, \pm 6$$

In Problems 12 – 14, use the Rational Zeros Theorem to find all the real zeros of each polynomial function. Use the zeros to factor  $f$  over the real numbers.

12.  $f(x) = x^3 - x^2 - 10x - 8$

$$P = \pm 1, \pm 2, \pm 4, \pm 8$$

$$Q = \pm 1$$

$$\begin{array}{r} -1 \mid 1 \ -1 \ -10 \ -8 \\ \quad \quad -1 \ 2 \ 8 \\ \hline 1 \ -2 \ -9 \ 0 \end{array}$$

$$(x+1)(x^2 - 2x - 8)$$

$$(x+1)(x-4)(x+2)$$

$$\{-1, 4, -2\}$$

$$13. f(x) = 4x^3 - 4x^2 - 7x - 2$$

$$\frac{P}{Q} = \left\{ \pm 1, \pm \frac{1}{2}, \pm \frac{1}{4}, \pm 2, \pm 4 \right\}$$

$$P = \pm 1, \pm 2$$

$$Q = \pm 1, \pm 2, \pm 4$$

$$\begin{array}{c} 4 \\ 2 \cancel{4} \\ \cancel{4} \end{array}$$

$$\begin{array}{r} 2 | 4 - 4 - 7 - 2 \\ \downarrow \quad 8 \quad 8 \quad 2 \\ \hline 4 \quad 4 \quad 1 \quad 0 \end{array}$$

$$(x-2)(4x^2 + 4x + 1)$$

$$(x-2)(2x+1)(2x+1)$$

$$\{2, -\frac{1}{2}\}$$

$-\frac{1}{2}$  Double root

$$14. f(x) = x^4 + 6x^3 + 11x^2 + 12x + 18$$

$$P = \pm 1, \pm 2, \pm 3, \pm 6, \pm 9, \pm 18$$

$$Q = \pm 1$$

$$\begin{array}{r} -3 | 1 \quad 6 \quad 11 \quad 12 \quad 18 \\ \quad \quad -3 \quad -9 \quad -6 \quad -18 \\ \hline \quad 1 \quad 3 \quad 2 \quad 6 \quad 0 \end{array}$$

$$(x+3)(x^3 + 3x^2 + 2x + 6)$$

-3